# A Gas Cartels in the Market, Hype or Reality?

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## Background

- In late 2018, Qatar left the OPEC
- The announcement stressed on the Gas market
- Qatar is a key player in the GECF
- The issues of Gas cartel formation again drew attentions

### **Basic Questions?**

- The Interaction Between Two Cartels and their members
- Which Countries Are Interested in Gas Cartel?
- Under Which Condition Gas Cartel agreement is Possible?
- The Effect of Gas Cartel Formation on P and Q of Oil and Gas

### **Countries Classification**

- ► I: Export only oil, OPEC members: KSA, Kuwait, Iraq.
- II: Export only oil, not members of OPEC: UK, Syria.
- III: Export both oil and NG and OPEC members: Qatar, Iran, Algeria, Nigeria, Venezuela.
- IV: Export both oil and NG, not members of OPEC: Oman, Canada, Russia, Norway.
- V: Export only NG: Turkmenistan, Ukraine, Uzbekistan, Bahrain.

### In The Model

- Group A: Export only oil, OPEC members: KSA, Kuwait, Iraq.
- Group B: Export both oil and NG, OPEC members: Qatar, Iran, Algeria, Nigeria, Venezuela.
- Group C: Export only NG: Turkmenistan, Ukraine, Uzbekistan, Bahrain.

#### **Demand Function**

$$P_i(Q_i, Q_j) = \alpha_i - \beta_i Q_i - \theta_i Q_j$$

for  $i, j \in \{O, G\}$  and  $i \neq j$ 

 $P_i$ : Price of product i

 $Q_i$ : Quantity of product i

 $Q_j$ : Quantity of product j

 $\alpha_i$ : Maximum price of product i (intercept)

 $\beta_i$ : Effect of the quantity of product i (direct effect)

 $\theta_i$ : Effect of the quantity of product j (indirect effect)

$$\beta_i, \beta_j \geq \theta_i, \theta_j \geq 0$$

### **Cost Function**

Marginal cost of production is constant and the same for all producers of a given good.

#### **Cartel Profit Function**

• When the cartel is formed, members try to maximize the sum of their profit, which includes their profit in substitute market,  $\lambda_A$  and  $\lambda_C$  show their share in each market profit.

### Cartel Profit Function (Cont.)

#### Scenario 1(base):

$$\pi_{OC}^{1} = \lambda_{A}\pi_{O} + (1 - \lambda_{A})\pi_{O} + \pi_{G,B}$$

$$\pi_{B}^{1} = (1 - \lambda_{A})\pi_{O} + \pi_{G,B}$$

$$\pi_{G,C}^{1} = q_{G,C}[(\alpha_{G} - \beta_{G}(q_{G,B} + q_{G,C}) - \theta_{G}Q_{O} - C_{G})]$$

#### Scenario 2:

$$\pi_{OC}^{2} = \lambda_{A}\pi_{O} + (1 - \lambda_{A})\pi_{O} + (1 - \lambda_{C})\pi_{G}$$

$$\pi_{GC}^{2} = \lambda_{C}\pi_{G} + (1 - \lambda_{A})\pi_{O} + (1 - \lambda_{C})\pi_{G}$$

# Stability of the Cartel and Bargaining Factors

- They form a cartel if they are better off in the cartel compared to staying out.
- $\pi_B^1 \leq \pi_B^2$  and  $\pi_C^1 \leq \pi_C^2$
- Agreement possibilities for cartel formation:
  - With money transfer
  - Without money transfer

# **Results** – The effect of Gas Cartel Formation on P and Q

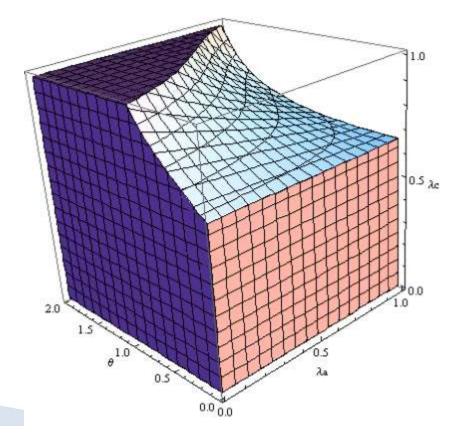
- Theorem 1: Following the formation of the gas cartel, for any sets of parameters:
- i) Q<sub>O</sub> increases
- ii) Q<sub>G</sub> decreases
- iii) P<sub>G</sub> increases
- Theorem 2:

The effects of the gas cartel formation on  $P_0$  is ambiguous.

### Results (Gas Cartel Formation Feasibility)

Theorem 3: There are some set of parameters such that there are no mutually beneficial political agreements.

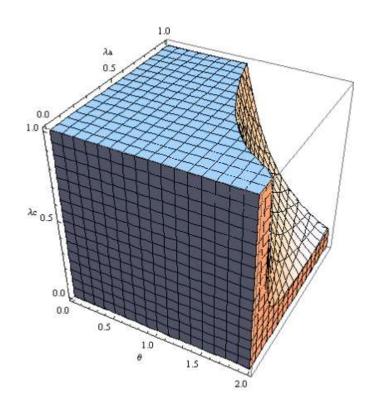
Values of  $\theta$ ,  $\lambda_A$ , and  $\lambda_C$  for which the oil price increases after the formation of the gas cartel with  $(\alpha=1,\beta=2,C=0)$ 



### Results (Gas Cartel Formation Feasibility)

Theorem 4: There are some set of parameters such that there are no mutually beneficial monetary agreements

Values of  $\theta$ ,  $\lambda_A$ , and  $\lambda_C$  for which mutually beneficial monetary agreement is possible with  $(\alpha=1,\beta=2$  and C=0)



### Conclusion

- In reality, since no money transfer is possible, the cartel formation is feasible only in narrow region of  $\lambda_C$  and  $\theta$ . Hence it vulnerable
- Findings implicitly indicate that  $\lambda_A$  is not a crucial factor impacting the formation of gas cartel.

### Conclusion (Cont.)

- powerful and active members of OPEC who are also key players of gas market prefer a joint strategy for both oil and gas.
- But countries that have unbalanced portfolio of oil and gas supply may not be interested to remain in both if there is an efficient gas cartel.

### **Future Works**

Including all five country groups and model their willingness to join the cartel and the effects of the new gas cartel on each group's profits.

# Thank you

#### Literature Review

- ► General Cartel Behavior and Its Stability
  Harrington (2005), Feurestein (2005), Iwarani et al.(2007),
  Villar (2004), Choi et al (2009)
- Applied (Gas Cartel Formation and Its Effect) Ehrman (2006), Egging et al.(2009), Gabriel et al. (2010)

## Method of Solving

- Four Different Level of Symmetric Parameter,
- Level One: all Parameters are symmetric except λ

$$\alpha_O = \alpha_G = \alpha$$
,  $\beta_O = \beta_G = \beta$ ,  $\theta_O = \theta_G = \theta$  and  $C_O = C_G = C$ 

- Level Two: Only  $\theta$  is Symmetric
- Level Three:  $\theta$  and  $\beta$  are Symmetric
- Level Four: All parameters are Asymmetric

# Equilibrium P, Q and Profits Scenario 1

$$\begin{split} Q_O^1 &= \frac{(\alpha - C) \ (\beta - \theta)}{2(\beta^2 - \theta^2) + \lambda_A \theta^2} \\ Q_{G,B}^1 &= \frac{(\alpha - C)(2\beta - \theta)(\beta + \theta(-1 + \lambda_A))}{3\beta(2(\beta^2 - \theta^2) + \lambda_A \theta^2)} \\ Q_{G,C}^1 &= \frac{(\alpha - C)(2(\beta^2 - \theta^2) + 2\theta^2\lambda_A - \beta\theta\lambda_A)}{3\beta(2(\beta^2 - \theta^2) + \lambda_A \theta^2)} \\ P_O^1 &= \frac{C(\beta + \theta(3\beta^2 - 2\beta\theta + \theta^2(-1 + \lambda_A))}{3\beta(2(\beta^2 - \theta^2) + \lambda_A \theta^2)} \\ &+ \frac{\alpha(3\beta^3 - \beta^2\theta - \theta^3(-1 + \lambda_A) + \beta\theta^2(-3 + 2\lambda_A))}{3\beta(2(\beta^2 - \theta^2) + \lambda_A \theta^2)} \\ P_G^1 &= \frac{C(\beta + \theta)(4\beta + \theta(-4 + \lambda_A)) + \alpha(2\beta^2 + 2\theta^2(-1 + \lambda_A) - \beta\theta\lambda_A)}{6\beta^2 + 3\theta^2(-2 + \lambda_A)} \end{split}$$

# Equilibrium P, Q and Profits Scenario 1 (Cont.)

$$\pi_{A}^{1} = \frac{(\alpha - C)^{2}(\beta - \theta)\lambda_{A}(3\beta^{3} - \beta^{2}\theta - \theta^{3}(-1 + \lambda_{A}) + \beta\theta^{2}(-3 + 2\lambda_{A}))}{3\beta(2(\beta^{2} - \theta^{2}) + \lambda_{A}\theta^{2})^{2}}$$

$$\pi_{B}^{1} = \frac{-(\alpha - C)^{2}(2\beta^{3}\theta(9 - 7\lambda_{A}) + 5\theta^{4}(-1 + \lambda_{A})^{2} + \beta^{4}(-13 + 9\lambda_{A}))}{9\beta(2(\beta^{2} - \theta^{2}) + \lambda_{A}\theta^{2})^{2}} + \frac{-(\alpha - C)^{2}(\beta^{2}\theta^{2}(8 + \lambda_{A}(-17 + 8\lambda_{A})) - 2\beta^{3}(-1 + \lambda_{A})(-9 + 7\lambda_{A}))}{9\beta(2(\beta^{2} - \theta^{2}) + \lambda_{A}\theta^{2})^{2}}$$

$$\pi_{C}^{1} = \frac{(\alpha - C)^{2}(2\beta^{2} + 2\theta^{2}(-1 + \lambda_{A}) - \beta\theta\lambda_{A})^{2}}{9\beta(2(\beta^{2} - \theta^{2}) + \lambda_{A}\theta^{2})^{2}}$$

# Equilibrium P, Q and Profits Scenario 2

$$Q_{O}^{2} = \frac{(\alpha - C)(2\beta + \theta(-2 + \lambda_{A}))}{4\beta^{2} - \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C})}$$

$$Q_{G}^{2} = \frac{(\alpha - C)(2\beta + \theta(-2 + \lambda_{C}))}{4\beta^{2} - \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C})}$$

$$P_{O}^{2} = \frac{-C(2\beta^{2} + \theta^{2}(-2 + \lambda_{A}) + \beta\theta\lambda_{C})}{-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C})} + \frac{\alpha(-2\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-1 + \lambda_{C}) + \beta\theta\lambda_{C})}{-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C})}$$

$$P_{G}^{2} = \frac{-C(2\beta^{2} + \theta^{2}(-2 + \lambda_{C}) + \beta\theta\lambda_{A})}{-4\beta^{2} + \theta^{2}(-2 + \lambda_{C})(-1 + \lambda_{A}) + \beta\theta\lambda_{A})} + \frac{\alpha(-2\beta^{2} + \theta^{2}(-2 + \lambda_{C})(-1 + \lambda_{A}) + \beta\theta\lambda_{A})}{-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C})}$$

# Equilibrium P, Q and Profits Scenario 2(Cont.)

$$\pi_{A}^{2} = \frac{\lambda_{A}(\alpha - C)^{2}(2(\beta - \theta) + \theta\lambda_{C}))(2\beta^{2} - \theta^{2}(-2 + \lambda_{A})(-1 + \lambda_{C}) - \beta\theta\lambda_{C})}{(-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C}))^{2}}$$

$$\pi_{B}^{2} = \frac{(\alpha - C)^{2}(2\theta^{3}(-2 + \lambda_{A})(-1 + \lambda_{A})(-2 + \lambda_{C})(-1 + \lambda_{C})}{(-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C}))^{2}} - \frac{(\alpha - C)^{2}(4\beta^{3}(-2 + \lambda_{A} + \lambda_{C}) + 4\beta^{2}\theta(-2 + \lambda_{A} + \lambda_{C}))}{(-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C}))^{2}} + \frac{(\alpha - C)^{2}\beta\theta^{2}(-8 + 3\lambda_{A}^{2}(-1 + \lambda_{C}) - 3(-4 + \lambda_{C})\lambda_{C})}{(-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C}))^{2}} - \frac{(\alpha - C)^{2}\beta\theta^{2}(\lambda_{A}(12 + \lambda_{C}(-16 + 3\lambda_{C})))}{(-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C}))^{2}}$$

$$\pi_{C}^{2} = \frac{\lambda_{C}(\alpha - C)^{2}(2(\beta - \theta) + \theta\lambda_{A}))(2\beta^{2} - \theta^{2}(-2 + \lambda_{C})(-1 + \lambda_{A}) - \beta\theta\lambda_{A})}{(-4\beta^{2} + \theta^{2}(-2 + \lambda_{A})(-2 + \lambda_{C}))^{2}}$$

# **Results** – The effect of Gas Cartel Formation on P and Q

- Theorem 01: Following the formation of the gas cartel, for any sets of parameters:
- i) Q<sub>o</sub> increases
- ii) Q<sub>G</sub> decreases
- iii) P<sub>G</sub> increases
- ▶ Theorem 02:

The effects of the gas cartel formation on Po is ambiguous.